

$$\log_9 (27 \cdot 81) = \log_9 (27) + \log_9 (81)$$

$$= \log_9 (9^{3/2}) + \log_9 (9^2)$$

Note:

$$27 = 3^3, \quad 9 = 3^2$$

$$\log_9 (27) = x$$

$$\Rightarrow 9^x = 27$$

$$\Rightarrow (3^2)^x = 3^3$$

$$\Rightarrow 3^{2x} = 3^3$$

$$\Rightarrow 2x = 3$$

$$\Rightarrow x = \frac{3}{2}$$

$$\checkmark \text{ check: } 9^{3/2} = (9^{1/2})^3 = (\sqrt{9})^3 = 3^3 = 27$$

$$= \frac{3}{2} \cdot \log_9 (9) + 2 \cdot \log_9 (9)$$

$$\text{Note}$$

$$\log_9 (9) = 1$$

$$= \frac{3}{2} + 2 = \frac{7}{2}$$